

MAT 300/500 Quiz 1 Answer Sheet

Spring 2022

Quiz ID: JST

Name: _____

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Submit electronic answers at

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MAT 300/500

Quiz 1

Spring 2022

- What is the dimension of the vector subspace of P_2 spanned by (consists of all linear combinations of) the polynomials t , $1 - t$, and $t(1 - t)$?
 a) 3 b) 2 c) 4 d) 1 e) 5
- What is the dimension of the vector subspace of P_3 which is spanned by the polynomials t^2 , and $(1 - t)^2$?
 a) 1 b) 2 c) 4 d) 2 e) 5
- Which polynomial has coordinate vector with respect to the standard basis $\{1, t, t^2\}$ equal to: $\begin{pmatrix} 1 \\ -2 \\ 0 \end{pmatrix}$.
 a) $(t + 2)^2$ b) $t^2 - (t - 1)^2$ c) $(t - 2)^2 + (t - 1)^2$ d) $(t - 1)^2 - t^2$ e) $(t + 1)^2$
- Let S be the set $\{(t - 4)^2, (t - 3)^2, t - 3\}$ of polynomials in P_2 . Determine whether the following statements are True or False. The answers are in order i),ii), iii).
 i) S is a top-down basis of P_2 ii) S spans P_2 iii) S is linearly independent
 a) TTF b) TTT c) FFF d) TTT e) FFT
- Let S be the set $\{(t - 1)^2, t - 1, t^2 - 1\}$ of polynomials in P_2 . Determine whether the following statements are True or False. The answers are in order i),ii), iii).
 i) S is a basis of P_2 ii) S spans P_2 iii) S is linearly independent
 a) TFF b) TFT c) FFF d) TTT e) FFT
- Which of the following are True statements about binomial coefficients, if $0 \leq k \leq d$?
 i) $\binom{d}{k} = \binom{d-1}{k} + \binom{d-1}{k-1}$ ii) $\binom{d}{k} = \binom{d}{d-k}$ iii) $\binom{d}{1} = d \binom{d}{0}$
 a) TFT b) FTT c) TTF d) TTT e) FTT
- Compute $\binom{4}{2} + \binom{4}{3}$:
 a) 7 b) 6 c) 10 d) 9 e) 8
- If V is a vector space with dimension $n - 1$, and $S = \{\mathbf{v}_1, \dots, \mathbf{v}_n\}$ is a set of n vectors in V then which of the following must be true:
 i) S cannot span V ii) S is a basis of V iii) S is linearly independent
 a) iii) only b) ii) and iii) only c) ii) only d) i) only e) i) and ii) only
- Find the coefficient of $t - 1$ in the polynomial $1 - (t - 2) + (t - 2)^2$ when converted to the shifted basis $\{1, t - 1, (t - 1)^2\}$.
 a) -6 b) -5 c) -3 d) -4 e) -2
- If A is the change of basis matrix from B_1 to B_2 and C is the change of basis matrix from B_1 to B_3 , then the change of basis matrix from B_3 to B_2 is:
 a) $(AC)^{-1}$ b) CA^{-1} c) AC d) $C^{-1}A^{-1}$ e) AC^{-1}