MAT 300/	500	Quiz 5	Answer Sheet				
Spring 2024							
Quiz ID:	MV	X		Name: _			
1.							
2.							
3.							
4.							
5.							
6.							
7.							
8.							
9.							
10.							

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		$\{6,6\}$, with associated quadratic <i>B</i> -splines where $\{a,b\}$ is a $\{a,b\}$ suppose that $\{a(t)\} = \sum_{i=1}^{11} P_i R^d(t)$ is a $\{a,b\}$ splines.			

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1.	Let t be the knot se	equence $\{-2, -1, 0, 1, $	1, 2, 2, 2, 3, 4, 4, 4, 6, 6, 6	}, with associated qua	adratic B -splines which
	are a basis of a vect	for space V of the for	f the form $P_{2,\mathbf{r}}^k[0,1,2,3,4,6]$. Suppose that $\gamma(t) = \sum_{i=1}^{11} P_i \mathcal{B}_i^d(t)$		
curve with control points P_0, \ldots, P_{11} . To compute $\gamma(3.5)$, what is the index J in the DeBoor algorithm (define by $t \in [t_J, t_{J+1})$)?					=0 Boor algorithm (defined
	a) 6	b) 9	c) 10	d) 7	e) 8
2. Same knot sequence \mathbf{t} and vector space V as in the previous question. Find the continuity vector \mathbf{r} .					uity vector r .
	a) $(0,1,0,-1)$	b) $(2,3,1,3)$	c) $(0,-1,1,-1)$	d) $(1,0,0,-1)$	e) $(2,-1,1,0)$
3. Same knot sequence \mathbf{t} and vector space V as in the previous question. Find the dimension of V .					
	a) 11	b) 10	c) 14	d) 13	e) 12
4.	Same knot sequence	\mathbf{t} and vector space V	as in the previous que	estion. Let S be the E	3-spline basis of V with

	a) 6	b) 7	c) 5	d) 8	e) 9	
5.	Same knot s	sequence \mathbf{t} and vector sp	ace V as in the prev	ious question. Let S	be the B -spline basis	of V with
knot sequence t. How many B-splines in S have exact order of continuity $r=1$ at $t=2$? (1)						exact order
	of continuity	of a B-spline $\mathcal{B}_i^d(t)$ at a	a knot value t_j is pre	dicted by the multipil	licty of t_j inside the s	sequence of
	knots $t_i, \ldots,$	t_{i+d+1} used to define the	ne B-spline $\mathcal{B}_i^{\bar{d}}(t)$.)		-	

6. Same knot sequence \mathbf{t} and vector space V as in the previous question. Let S be the B-spline basis of V with knot sequence \mathbf{t} . How many B-splines in S have exact order of continuity r = 1 at t = 3?

d) 3

e) 5

a) 1 b) 2 c) 4 d) 3 e) 5

knot sequence \mathbf{t} . How many B-splines in S are zero for all t in the interval [2,3]?

b) 2

a) 1

- 7. Which sequence of four knots will result in a quadratic B-spline which is continuous and consists of two parabolas which meet at a point which is the only place where the function is not differentiable?
 - a) 0,0,1,2 b) 0,0,0,1 c) 0,0,1,1 d) 0,1,2,2 e) 0,1,1,2
- 8. Which sequence of four knots will result in a quadratic *B*-spline which is continuous and differentiable except at one point, where it is continuous but not differentiable, and consists of two parabolas one of which is concave up and the other concave down?
 - a) 0,0,1,2 b) 0,0,0,1 c) 0,0,1,1 d) 0,1,2,2 e) 0,1,1,2
- 9. Which sequence of four knots will result in a quadratic B-spline which is continuous and which consists of only one parabola?
 - a) 0,0,1,2 b) 0,0,0,1 c) 0,0,1,1 d) 0,1,2,2 e) 0,1,1,2
- 10. Which sequence of five knots will result in a cubic B-spline which is continuous, but fails to have a continuous first derivative?
 - $a) \ \ 0,0,1,1,2 \\ \qquad b) \ \ 0,1,1,1,1 \\ \qquad c) \ \ 0,0,0,1,2 \\ \qquad d) \ \ 0,1,1,2,2 \\ \qquad e) \ \ 0,1,1,2,3 \\$