MAT	320
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Quiz 1

Fall 2023

Quiz ID:	QDC

Name: _____

Answers:

- 1.
- 2.
- 3.
- 4.
- 5.
- 6.
- 7.
- 8.
- 9.
- 10.

Submit electronic answers at

http://azrael.digipen.edu/cgi-bin/MAT320quiz.pl

MAT 320

Quiz 1

Fall 2023

1.	Factor the	e polynomial	p(x) = x	$x^3 + 1$	into	line ar	and	${\it quadratic}$	factors.	The	quadratic	factor
	is:											

a) $x^2 + 1$ b) $x^2 + x + 1$ c) $x^2 - x - 1$ d) $x^2 - x + 1$ e) $x^2 + x - 1$

2. Same polynomial p(x) as in the previous question. Use the quadratic formula to find the two complex roots of the quadratic factor. One of them is:

a) $\frac{1}{4} + \frac{\sqrt{3}}{4}i$ b) $\frac{1}{4} - \frac{\sqrt{3}}{4}i$ c) $\frac{1}{2} - \frac{\sqrt{3}}{2}i$ d) $1 + \sqrt{3}i$ e) $-\frac{1}{2} - \frac{\sqrt{3}}{2}i$

3. Let q(x) = (x - (a + bi))(x - (a - bi)) be a quadratic polynomial in factored form. Multiply out so that $q(x) = x^2 + c_1 x + c_0$. What is c_1 ?

a) 2a + 2bi

b) a + bi c) -2a d) $a^2 + b^2$ e) -2bi

4. Same polynomial q(x) as in the previous question. What is c_0 ?

a) 2a + 2bi b) a + bi c) -2a d) $a^2 + b^2$

e) -2bi

5. Let $f(t) = e^{i4\pi t}$ be a phasor defined for all real numbers t, where t represents time in seconds. What is the frequency of this phasor measured in Hz (cycles per second).

a) 4π

b) 4

c) 2

e) 2π

6. Same f(t) as in the previous question. What is the (smallest positive) period of f?

a) 4π

b) 4

c) 2

d) $\frac{1}{2}$

7. Let $f_c(z)$ be a complex function $f: \mathbb{C} \to \mathbb{C}$ which multiples the input complex variable z by the constant complex number c = a + bi. Assume f rotates z by an angle 120 degrees, or $\frac{2}{3}\pi$ radians, counterclockwise, and use this to solve for c. What is the real part a?

a) 1

c) 2

8. Same $f_c(z)$ as in the previous question. Find the Cartesian form for $f(e^{i\pi/3})$.

b) $\frac{1}{2} + \frac{\sqrt{3}}{2}i$ c) $-\frac{1}{2} + \frac{\sqrt{3}}{2}i$ d) -1 e) $-\frac{1}{2} - \frac{\sqrt{3}}{2}i$

9. Let $g(z) = \frac{1}{|z|}$ so that $g : \mathbb{C} \to \mathbb{R}$. Find g(1+i).

a) $\sqrt{2}$

b) $\frac{1}{2}$

c) $\frac{\sqrt{2}}{2}$

d) 1

e) $\frac{3}{2}$

10. Same g(z) as in the previous question. Find the maximum value of g(z) for inputs z = x + yiwhere y = x - 1.

a) $\sqrt{2}$

b) $\frac{1}{2}$

c) $\frac{\sqrt{2}}{2}$

d) 1

e) $\frac{3}{2}$